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An Introduction to the Interval Template Library

Lecture
held at the Boost Library Conference 2009

2009-05-08

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Lecture Outline

- Background and Motivation
- Design
- Examples
- Semantics
- Implementation
- Future Works
- Availability

Background and Motivation

- Interval containers simplified the implementation of date and time related tasks
  - Decomposing *“histories”* of attributed events into segments with constant attributes.
  - Working with time grids, e.g. a grid of months.
  - Aggregations of values associated to date or time intervals.

- … that occurred frequently in programs like
  - Billing modules
  - Therapy scheduling programs
  - Hospital and controlling statistics

Design

- Background is the date time problem domain ...
- … but the scope of the **itl** as a generic library is more general:

an **interval_set** *is a* **set**

that is implemented as a set of intervals

an **interval_map** *is a* **map**

that is implemented as a map of interval value pairs

Aspects

- There are two aspects in the design of interval containers
- Conceptual aspect

```
interval_set<int> mySet;
mySet.insert(42);
bool has_answer = mySet.contains(42);
```

  - On the conceptual aspect an interval_set can be used just as a set of elements
  - except for . . .
  - . . . ***iteration*** *over elements*
  - consider `interval_set<double>` or `interval_set<string>`
- Iterative Aspect
  - **Iteration** is always done over *intervals*

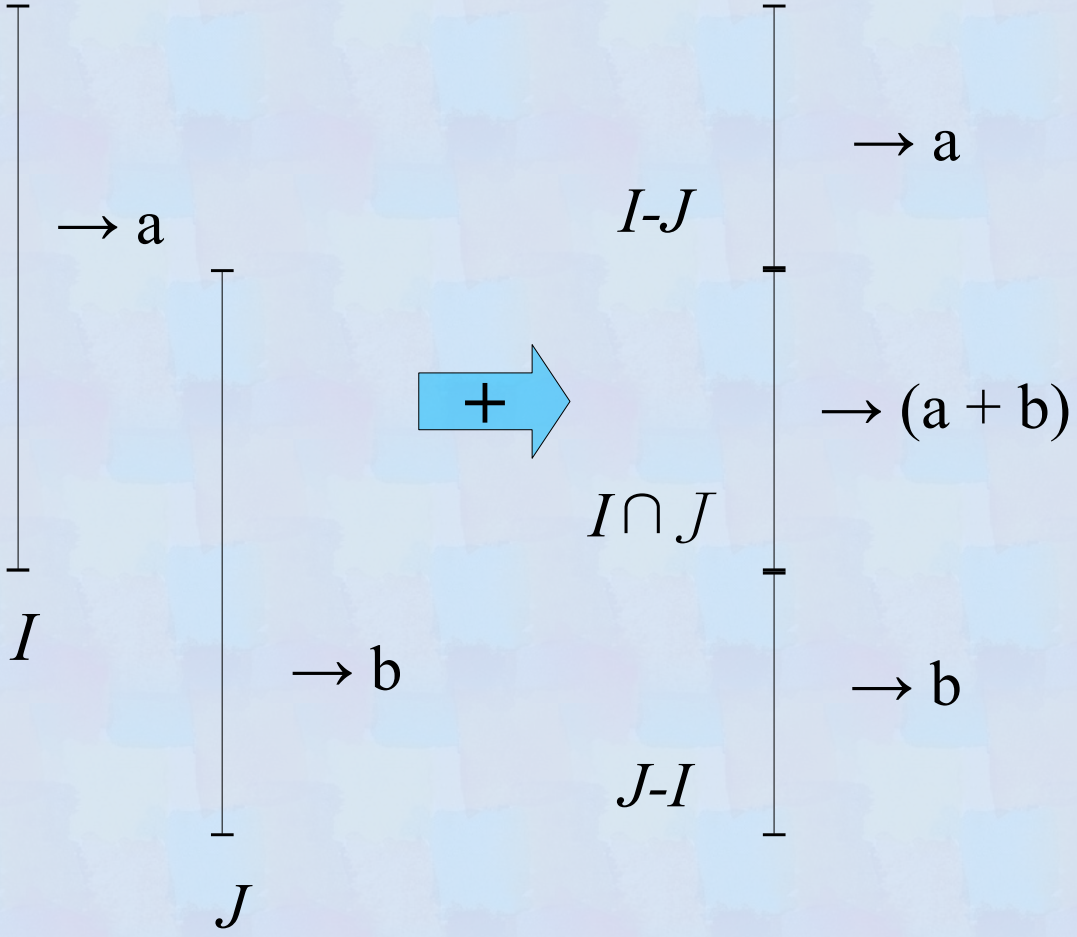
Design

- Addability and Subtractability
  - All of itl's (interval) containers are *Addable* and *Subtractable*
  - They implement `operators +=, +, -=` and `-`

	`+=`	`-=`
sets	set union	set difference
maps	?	?

- A possible implementation for maps
  - Propagate addition/subtraction to the associated values
  - . . . or aggregate on overlap
  - . . . or aggregate on collision

- Aggregate on overlap



- Decompositional effect on Intervals
- Accumulative effect on associated values

I, J: intervals, a,b: associated values

- Aggregate on overlap, a minimal example

```
typedef itl::set<string> guests;
interval_map<time, guests> party;

party += make_pair(
  interval<time>::rightopen(20:00, 22:00), guests("Mary"));

party += make_pair(
  interval<time>::rightopen(21:00, 23:00), guests("Harry"));


// party now contains
[20:00, 21:00)->{"Mary"}
[21:00, 22:00)->{"Harry","Mary"} //guest sets aggregated
[22:00, 23:00)->{"Harry"}
```

- The Itl's class templates

Granu-larity	Style	Sets	Maps
interval		`interval`	
	joining	`interval_set`	`interval_map`
	separating	`separate_interval_set`	
	splitting	`split_interval_set`	`split_interval_map`
element		`set`	`map`

- Interval Combining Styles: ***Joining***
  - Intervals are joined on overlap or on touch
  - . . . *for maps*, if associated values are equal
  - Keeps interval_maps and sets in a minimal form

interval_set

```
   {[1        3)              }
+         [2        4)
+                     [4  5)

= {[1                 4)       }

= {[1                       5)}
```

interval_map

```
   {[1        3)->1           }
+         [2        4)->1
+                     [4  5)->1

={[1 2)[2 3)[3 4)             }
    ->1   ->2   ->1
={[1 2)[2 3)[3        5)      }
    ->1   ->2       ->1
```

- Interval Combining Styles: ***Splitting***
  - Intervals are split on overlap and kept separate on touch
  - All interval borders are preserved (insertion memory)

split_interval_set

```
  {[1       3)             }
+       [2       4)
+                  [4 5)

= {[1 2)[2 3)[3 4)       }

= {[1 2)[2 3)[3 4)[4 5)}
```

split_interval_map

```
  {[1       3)->1          }
+       [2       4)->1
+                  [4 5)->1

={[1 2)[2 3)[3 4)          }
   ->1  ->2  ->1
={[1 2)[2 3)[3 4)[4 5)     }
   ->1  ->2  ->1  ->1
```

- Interval Combining Styles: ***Separating***
  - Intervals are joined on overlap but kept separate on touch
  - Preserves borders that are never crossed (preserves a hidden grid).

```
separate_interval_set

   {[1        3)              }
+         [2        4)
+                     [4  5)

= {[1               4)       }

= {[1               4)[4  5)}
```

Examples

- A few instances of intervals (interval.cpp)

```
interval<int> int_interval = interval<int>::closed(3,7);

interval<double> sqrt_interval
  = interval<double>::rightopen(1/sqrt(2.0), sqrt(2.0));

interval<std::string> city_interval
  = interval<std::string>::leftopen("Barcelona", "Boston");

interval<boost::ptime> time_interval
  = interval<boost::ptime>::open(
                        time_from_string("2008-05-20 19:30"),
                        time_from_string("2008-05-20 23:00")
    );
```

Examples

- A way to iterate over months and weeks (month_and_week_grid.cpp)

```
#include <boost/itl/gregorian.hpp> //boost::gregorian plus adapter code
#include <boost/itl/split_interval_set.hpp>

// A split_interval_set of gregorian dates as date_grid.
typedef split_interval_set<boost::gregorian::date> date_grid;

// Compute a date_grid of months using boost::gregorian.
date_grid month_grid(const interval<date>& scope)
{
    date_grid month_grid;
    // Compute a date_grid of months using boost::gregorian.
    . . .
    return month_grid;
}

// Compute a date_grid of weeks using boost::gregorian.
date_grid week_grid(const interval<date>& scope)
{
    date_grid week_grid;
    // Compute a date_grid of weeks using boost::gregorian.
    . . .
    return week_grid;
}
```

Examples

- A way to iterate over months and weeks

```
void month_and_time_grid()
{
    date someday = day_clock::local_day();
    date thenday = someday + months(2);
    interval<date> scope = interval<date>::rightopen(someday, thenday);

    // An intersection of the month and week grids ...
    date_grid month_and_week_grid
        = month_grid(scope) & week_grid(scope);

    // ... allows to iterate months and weeks. Whenever a month
    // or a week changes there is a new interval.
    for(date_grid::iterator it = month_and_week_grid.begin();
        it != month_and_week_grid.end(); it++)
    {   . . .   }

    // We can also intersect the grid into an interval_map to make
    // shure that all intervals are within months and week bounds.
    interval_map<boost::gregorian::date, some_type> accrual;
    compute_some_result(accrual, scope);
    accrual &= month_and_week_grid;

}
```

Examples

- Aggregating with interval_maps
  - Computing averages via implementing **operator +=** (partys_guest_average.cpp)

```
class counted_sum
{
public:
    counted_sum():_sum(0),_count(0){}
    counted_sum(int sum):_sum(sum),_count(1){}

    int sum()const  {return _sum;}
    int count()const{return _count;}
    double average()const
    { return _count==0 ? 0.0 : _sum/static_cast<double>(_count); }

    counted_sum& operator += (const counted_sum& right)
    { _sum += right.sum(); _count += right.count(); return *this; }

private:
    int _sum;
    int _count;
};

bool operator == (const counted_sum& left, const counted_sum& right)
{ return left.sum()==right.sum() && left.count()==right.count(); }
```

Examples

- Aggregating with interval_maps
  - Computing averages via implementing **operator +=**

```
void partys_height_average()
{
    interval_map<ptime, counted_sum> height_sums;

    height_sums += (
      make_pair(
        interval<ptime>::rightopen(
          time_from_string("2008-05-20 19:30"),
          time_from_string("2008-05-20 23:00")),
          counted_sum(165)) // Mary is 1,65 m tall.
    );

    // Add height of more pary guests . . .

    interval_map<ptime, counted_sum>::iterator height_sum_ =
        height_sums.begin();
    while(height_sum_ != height_sums.end())
    {
        interval<ptime> when = height_sum_->first;
        double height_average = (*height_sum_++).second.average();

        cout << "[" << when.first() << " - " << when.upper() << ")"
             << ": " << height_average << " cm" << endl;
    }
}
```

Examples

- Interval containers allow to express a variety of date and time operations in an easy way.
  - Example **man_power.cpp ...**
  - Subtract weekends and holidays from an interval_set

```
worktime -= weekends(scope)
worktime -= german_reunification_day
```

  - Intersect an interval_map with an interval_set

```
claudias_working_hours &= worktime
```

  - Subtract and interval_set from an interval map

```
claudias_working_hours -= claudias_absense_times
```

  - Adding interval_maps

```
interval_map<date,int> manpower;
manpower += claudias_working_hours;
manpower += bodos_working_hours;
```

Examples

- Interval_maps can also be intersected
  Example **`user_groups.cpp`**

```
typedef boost::itl::set<string> MemberSetT;
typedef interval_map<date, MemberSetT> MembershipT;

void user_groups()
{
    . . .

    MembershipT med_users;
    // Compute membership of medical staff
    med_users += make_pair(member_interval_1, MemberSetT("Dr.Jekyll"));
    med_users += . . .

    MembershipT admin_users;
    // Compute membership of administation staff
    med_users += make_pair(member_interval_2, MemberSetT("Mr.Hyde"));
    . . .

    MembershipT all_users   = med_users + admin_users;

    MembershipT super_users = med_users & admin_users;
    . . .

}
```

Semantics

- The semantics of ***itl sets*** is based on a concept **`itl::Set`**
  - **`itl::set`**, **`interval_set`**, **`split_interval_set`** and **`separate_interval_set`** are models of concept **`itl::Set`**

```
// Abstract part
empty set:          Set::Set()
subset relation:    bool Set::contained_in(const Set& s2)const
equality:           bool is_element_equal(const Set& s1, const Set& s2)
set union:          Set& operator += (Set& s1, const Set& s2)
                    Set  operator +  (const Set& s1, const Set& s2)
set difference:     Set& operator -= (Set& s1, const Set& s2)
                    Set  operator -  (const Set& s1, const Set& s2)
set intersection:   Set& operator &= (Set& s1, const Set& s2)
                    Set  operator &  (const Set& s1, const Set& s2)

// Part related to sequential ordering
sorting order:      bool operator <  (const Set& s1, const Set& s2)
lexicographical equality:
                    bool operator == (const Set& s1, const Set& s2)
```

Semantics

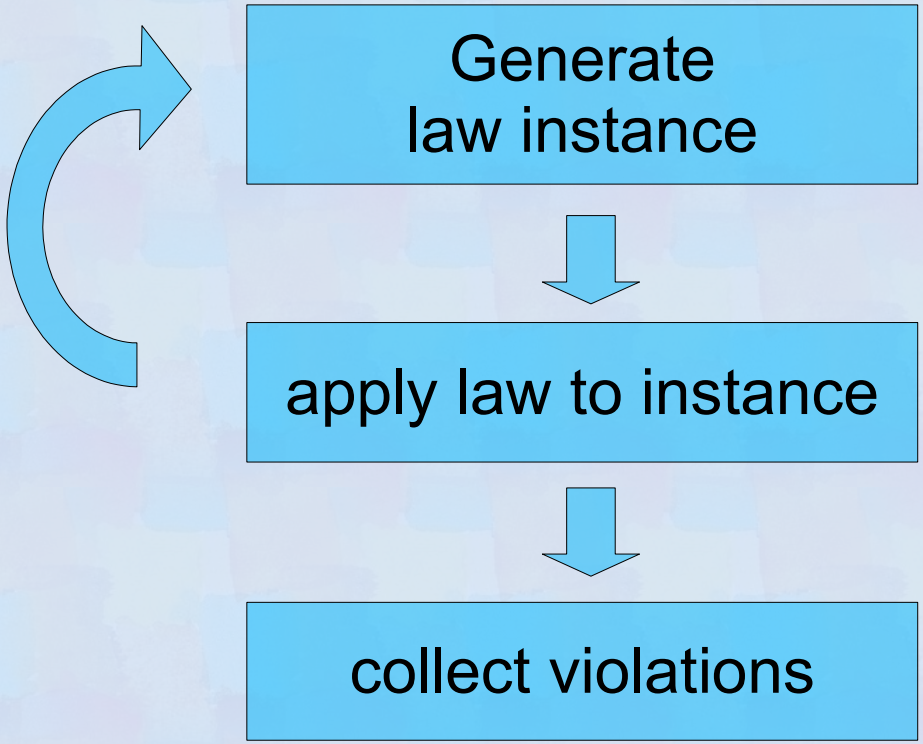
- The semantics of ***itl maps*** is based on a concept **`itl::Map`**
  - **`itl::map`**, **`interval_map`** and **`split_interval_map`** are models of concept **`itl::Map`**

```
// Abstract part
empty map:          Map::Map()
submap relation:    bool Map::contained_in(const Map& m2)const
equality:           bool is_element_equal(const Map& m1, const Map& m2)
map union:          Map& operator += (Map& m1, const Map& m2)
                    Map  operator +  (const Map& m1, const Map& m2)
map difference:     Map& operator -= (Map& m1, const Map& m2)
                    Map  operator -  (const Map& m1, const Map& m2)
map intersection:   Map& operator &= (Map& m1, const Map& m2)
                    Map  operator &  (const Map& m1, const Map& m2)

// Part related to sequential ordering
sorting order:      bool operator <  (const Map& m1, const Map& m2)
lexicographical equality:
                    bool operator == (const Map& m1, const Map& m2)
```

Semantics

- Defining semantics of itl concepts via sets of laws
  - aka c++0x axioms
- Checking law sets via automatic testing:
  - A ***La***w ***Ba***sed ***Te***st ***A***utomaton ***LaBatea***




```
Commutativity<T a, U b, +>:
  a + b = b + a;
```

Semantics

- Lexicographical Ordering and Equality
  - For all itl containers `operator <` implements a ***strict weak ordering***.
  - The ***induced equivalence*** of this ordering is ***lexicographical equality*** which is implemented as `operator ==`
  - This is in line with the semantics of SortedAssociativeContainers

Semantics

- Subset Ordering and Element Equality
  - For all itl containers function `contained_in` implements a ***partial ordering***.
  - The ***induced equivalence*** of this ordering is ***equality of elements*** which is implemented as function `is_element_equal`.

Semantics

- itl::Sets
- All itl sets implement a ***Set Algebra***, which is to say satisfy a "*classical*" set of laws . . .
  - . . . using `is_element_equal` as equality
  - Associativity, Neutrality, Commutativity (for + and &)
  - Distributivity, DeMorgan, Symmetric Difference
- Most of the itl sets satisfy the classical set of laws even if . . .
  - . . . lexicographical equality: `operator ==` is used
  - The differences reflect proper inequalities in sequence that occur for `separate_interval_set` and `split_interval_set`.

Semantics

- Concept Induction / Concept Transition
  - The semantics of itl::Maps appears to be *determined* by the *codomain type* of the map

	is model of	*if*	example
`Map<D,Monoid>`	`Monoid`		`interval_map<int,string>`
`Map<D,Set>`	`Set`	*C1*	`interval_map<int,set<int>>`
`Map<D,CommutMonoid>`	`CommutMonoid`		`interval_map<int,unsigned>`
`Map<D,AbelianGroup>`	`AbelianGroup`	*C2*	`interval_map<int,int,`*`total`*`>`

  - Conditions ***C1*** and ***C2*** restrict the *Concept Induction* to specific *map traits*
    - ***C1***: Value pairs that carry a *neutral element* as associated value are always deleted (Trait: ***absorbs_neutrons***).
    - ***C2***: The map *is total*: Non existing keys are implicitly mapped to *neutral elements* (Trait: ***is_total***).

Implementation

- Itl containers are implemented based on std::set and std::map
  - Basic operations like *adding* and *subtracting* intervals or interval value pairs perform with a time *complexity between** *amortized O(log n)* and *O(n)*, where *n* is the number of intervals of a container.
  - Operations like *addition* and *subtraction* of whole containers are having a worst case complexity of *O(m log(n+m))*, where *n* and *m* are the numbers of intervals of the containers to combine.

  * : Consult the library documentation for more detailed information.

Future Works

- Implementing interval_maps of sets more efficiently
- Revision of features of the extended itl (itl_plus.zip)
  - Decomposition of histories: k histories h_k with attribute types $A_1, ..., A_k$ are "*decomposed*" to a product history of tuples of attribute sets:
    $(h_1<T,A_1>,..., h<T,A_k>) \rightarrow h<T, (set<A_1>,\ldots, set<A_k>)>$
  - Cubes (generalized crosstables): Applying *aggregate on collision* to maps of tuple value pairs in order to organize hierachical data and their aggregates.

Availability

- Itl project on sourceforge (version 2.0.1)
  http://sourceforge.net/projects/itl
- Latest version on boost vault/Containers (3.1.0)
  http://www.boostpro.com/vault/ → containers
  - itl_3_1_0.zip : Core itl in preparation for boost
  - itl_plus_3_1_0.zip : Extended itl including histories, cubes and automatic validation (LaBatea).
- Online documentation at
  http://www.herold-faulhaber.de/
  - Doxygen generated docs for (version 2.0.1)
    http://www.herold-faulhaber.de/itl/
  - Latest boost style documentation (version 3.1.0)
    http://www.herold-faulhaber.de/boost_itl/doc/libs/itl/doc/html/

Availability

- Boost sandbox
  https://svn.boost.org/svn/boost/sandbox/itl/
  - Core itl: Interval containers in prepartion for boost
    https://svn.boost.org/svn/boost/sandbox/itl/boost/itl/
    https://svn.boost.org/svn/boost/sandbox/itl/libs/itl/
  - Extended itl_xt: “histories” and cubes
    https://svn.boost.org/svn/boost/sandbox/itl/boost/itl_xt/
    https://svn.boost.org/svn/boost/sandbox/itl/libs/itl_xt/
  - Validater LaBatea:
    Compiles with msvc-8.0 or newer, gcc-4.3.2 or newer
    https://svn.boost.org/svn/boost/sandbox/itl/boost/validate/
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- … that occurred frequently in programs like
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an **interval_map** *is a* **map**

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  - On the conceptual aspect an interval_set can be used just as a set of elements
  - except for . . .
  - . . . ***iteration*** *over elements*
  - consider **`interval_set<double>`** or **`interval_set<string>`**
- Iterative Aspect
  - **Iteration** is always done over *intervals*

Design

- Addability and Subtractability
  - All of itl's (interval) containers are *Addable* and *Subtractable*
  - They implement `operators +=, +, -=` and `-`

	`+=`	`-=`
sets	set union	set difference
maps	?	?

- A possible implementation for maps
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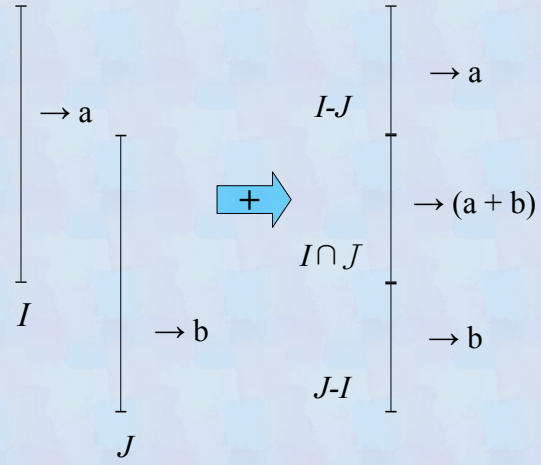
  - . . . or aggregate on collision

Design

- Aggregate on overlap



- Decompositional effect on Intervals
- Accumulative effect on associated values

I, J: intervals, a,b: associated values

- Aggregate on overlap, a minimal example

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typedef itl::set<string> guests;
interval_map<time, guests> party;

party += make_pair(
  interval<time>::rightopen(20:00, 22:00), guests("Mary"));

party += make_pair(
  interval<time>::rightopen(21:00, 23:00), guests("Harry"));


// party now contains
[20:00, 21:00)->{"Mary"}
[21:00, 22:00)->{"Harry","Mary"} //guest sets aggregated
[22:00, 23:00)->{"Harry"}
```

Design

- The Itl's class templates

Granu-larity	Style	Sets	Maps
interval		`interval`	
	joining	`interval_set`	`interval_map`
	separating	`separate_interval_set`	
	splitting	`split_interval_set`	`split_interval_map`
element		`set`	`map`

- Interval Combining Styles: ***Joining***
  - Intervals are joined on overlap or on touch
  - . . . *for maps*, if associated values are equal
  - Keeps interval_maps and sets in a minimal form

interval_set

```
  {[1       3)           }
+       [2       4)
+                  [4 5)

= {[1            4)      }

= {[1                 5)}
```

interval_map

```
  {[1       3)->1        }
+       [2       4)->1
+                  [4 5)->1

={[1 2)[2 3)[3 4)        }
   ->1  ->2  ->1
={[1 2)[2 3)[3       5)  }
   ->1  ->2     ->1
```

- Interval Combining Styles: ***Splitting***
  - Intervals are split on overlap and kept separate on touch
  - All interval borders are preserved (insertion memory)

split_interval_set

```
  {[1       3)           }
+       [2       4)
+                  [4 5)

= {[1 2)[2 3)[3 4)      }

= {[1 2)[2 3)[3 4)[4 5)}
```

split_interval_map

```
  {[1       3)->1          }
+       [2       4)->1
+                  [4 5)->1

={[1 2)[2 3)[3 4)         }
   ->1  ->2  ->1
={[1 2)[2 3)[3 4)[4 5)    }
   ->1  ->2  ->1  ->1
```

- Interval Combining Styles: ***Separating***
  - Intervals are joined on overlap but kept separate on touch
  - Preserves borders that are never crossed (preserves a hidden grid).

```
separate_interval_set

  {[1       3)           }
+       [2       4)
+                  [4 5)

= {[1             4)      }

= {[1             4)[4 5)}
```

Examples

- A few instances of intervals (interval.cpp)

```
interval<int> int_interval = interval<int>::closed(3,7);

interval<double> sqrt_interval
  = interval<double>::rightopen(1/sqrt(2.0), sqrt(2.0));

interval<std::string> city_interval
  = interval<std::string>::leftopen("Barcelona", "Boston");

interval<boost::ptime> time_interval
  = interval<boost::ptime>::open(
                        time_from_string("2008-05-20 19:30"),
                        time_from_string("2008-05-20 23:00")
    );
```

Examples

- A way to iterate over months and weeks (month_and_week_grid.cpp)

```
#include <boost/itl/gregorian.hpp> //boost::gregorian plus adapter code
#include <boost/itl/split_interval_set.hpp>

// A split_interval_set of gregorian dates as date_grid.
typedef split_interval_set<boost::gregorian::date> date_grid;

// Compute a date_grid of months using boost::gregorian.
date_grid month_grid(const interval<date>& scope)
{
    date_grid month_grid;
    // Compute a date_grid of months using boost::gregorian.
    . . .
    return month_grid;
}

// Compute a date_grid of weeks using boost::gregorian.
date_grid week_grid(const interval<date>& scope)
{
    date_grid week_grid;
    // Compute a date_grid of weeks using boost::gregorian.
    . . .
    return week_grid;
}
```

Examples

- A way to iterate over months and weeks

```
void month_and_time_grid()
{
    date someday = day_clock::local_day();
    date thenday = someday + months(2);
    interval<date> scope = interval<date>::rightopen(someday, thenday);

    // An intersection of the month and week grids ...
    date_grid month_and_week_grid
        = month_grid(scope) & week_grid(scope);

    // ... allows to iterate months and weeks. Whenever a month
    // or a week changes there is a new interval.
    for(date_grid::iterator it = month_and_week_grid.begin();
        it != month_and_week_grid.end(); it++)
    {   . . .   }

    // We can also intersect the grid into an interval_map to make
    // shure that all intervals are within months and week bounds.
    interval_map<boost::gregorian::date, some_type> accrual;
    compute_some_result(accrual, scope);
    accrual &= month_and_week_grid;

}
```

Examples

- Aggregating with interval_maps
  - Computing averages via implementing **operator +=** (partys_guest_average.cpp)

```
class counted_sum
{
public:
    counted_sum():_sum(0),_count(0){}
    counted_sum(int sum):_sum(sum),_count(1){}

    int sum()const  {return _sum;}
    int count()const{return _count;}
    double average()const
    { return _count==0 ? 0.0 : _sum/static_cast<double>(_count); }

    counted_sum& operator += (const counted_sum& right)
    { _sum += right.sum(); _count += right.count(); return *this; }

private:
    int _sum;
    int _count;
};

bool operator == (const counted_sum& left, const counted_sum& right)
{ return left.sum()==right.sum() && left.count()==right.count(); }
```

Examples

- Aggregating with interval_maps
  - Computing averages via implementing **operator +=**

```
void partys_height_average()
{
    interval_map<ptime, counted_sum> height_sums;

    height_sums += (
      make_pair(
        interval<ptime>::rightopen(
          time_from_string("2008-05-20 19:30"),
          time_from_string("2008-05-20 23:00")),
          counted_sum(165)) // Mary is 1,65 m tall.
    );

    // Add height of more pary guests . . .

    interval_map<ptime, counted_sum>::iterator height_sum_ =
        height_sums.begin();
    while(height_sum_ != height_sums.end())
    {
        interval<ptime> when = height_sum_->first;
        double height_average = (*height_sum_++).second.average();

        cout << "[" << when.first() << " - " << when.upper() << ")"
             << ": " << height_average << " cm" << endl;
    }
}
```

Examples

- Interval containers allow to express a variety of date and time operations in an easy way.
  - Example `man_power.cpp ...`
  - Subtract weekends and holidays from an interval_set
    ```
    worktime -= weekends(scope)
    worktime -= german_reunification_day
    ```
  - Intersect an interval_map with an interval_set
    ```
    claudias_working_hours &= worktime
    ```
  - Subtract and interval_set from an interval map
    ```
    claudias_working_hours -= claudias_absense_times
    ```
  - Adding interval_maps
    ```
    interval_map<date,int> manpower;
    manpower += claudias_working_hours;
    manpower += bodos_working_hours;
    ```

Examples

- Interval_maps can also be intersected
  Example **`user_groups.cpp`**

```
typedef boost::itl::set<string> MemberSetT;
typedef interval_map<date, MemberSetT> MembershipT;

void user_groups()
{
    . . .

    MembershipT med_users;
    // Compute membership of medical staff
    med_users += make_pair(member_interval_1, MemberSetT("Dr.Jekyll"));
    med_users += . . .

    MembershipT admin_users;
    // Compute membership of administation staff
    med_users += make_pair(member_interval_2, MemberSetT("Mr.Hyde"));
    . . .

    MembershipT all_users   = med_users + admin_users;

    MembershipT super_users = med_users & admin_users;
    . . .

}
```

Semantics

- The semantics of ***itl sets*** is based on a concept **`itl::Set`**
  - **`itl::set`**, **`interval_set`**, **`split_interval_set`** and **`separate_interval_set`** are models of concept **`itl::Set`**

```
// Abstract part
empty set:         Set::Set()
subset relation:   bool Set::contained_in(const Set& s2)const
equality:          bool is_element_equal(const Set& s1, const Set& s2)
set union:         Set& operator += (Set& s1, const Set& s2)
                   Set  operator +  (const Set& s1, const Set& s2)
set difference:    Set& operator -= (Set& s1, const Set& s2)
                   Set  operator -  (const Set& s1, const Set& s2)
set intersection:  Set& operator &= (Set& s1, const Set& s2)
                   Set  operator &  (const Set& s1, const Set& s2)

// Part related to sequential ordering
sorting order:     bool operator <  (const Set& s1, const Set& s2)
lexicographical equality:
                   bool operator == (const Set& s1, const Set& s2)
```

Semantics

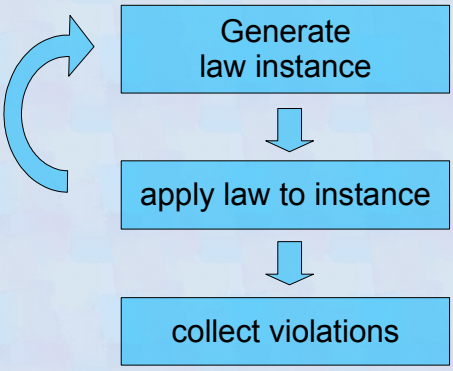
- The semantics of ***itl maps*** is based on a concept **`itl::Map`**
  - **`itl::map`**, **`interval_map`** and **`split_interval_map`** are models of concept **`itl::Map`**

```
// Abstract part
empty map:          Map::Map()
submap relation:    bool Map::contained_in(const Map& m2)const
equality:           bool is_element_equal(const Map& m1, const Map& m2)
map union:          Map& operator += (Map& m1, const Map& m2)
                    Map  operator +  (const Map& m1, const Map& m2)
map difference:     Map& operator -= (Map& m1, const Map& m2)
                    Map  operator -  (const Map& m1, const Map& m2)
map intersection: Map& operator &= (Map& m1, const Map& m2)
                    Map  operator &  (const Map& m1, const Map& m2)

// Part related to sequential ordering
sorting order:      bool operator <  (const Map& m1, const Map& m2)
lexicographical equality:
                    bool operator == (const Map& m1, const Map& m2)
```

Semantics

- Defining semantics of itl concepts via sets of laws
  - aka c++0x axioms
- Checking law sets via automatic testing:
  - A ***La***w ***Ba***sed ***Te***st ***A***utomaton ***LaBatea***




```
Commutativity<T a, U b, +>:
a + b = b + a;
```

Semantics

- Lexicographical Ordering and Equality
  - For all itl containers `operator <` implements a ***strict weak ordering***.
  - The ***induced equivalence*** of this ordering is ***lexicographical equality*** which is implemented as `operator ==`
  - This is in line with the semantics of SortedAssociativeContainers

Semantics

- Subset Ordering and Element Equality
  - For all itl containers function `contained_in` implements a ***partial ordering***.
  - The ***induced equivalence*** of this ordering is ***equality of elements*** which is implemented as function `is_element_equal`.

Semantics

- itl::Sets
- All itl sets implement a ***Set Algebra***, which is to say satisfy a "*classical*" set of laws . . .
  - . . . using `is_element_equal` as equality
  - Associativity, Neutrality, Commutativity (for + and &)
  - Distributivity, DeMorgan, Symmetric Difference
- Most of the itl sets satisfy the classical set of laws even if . . .
  - . . . lexicographical equality: `operator ==` is used
  - The differences reflect proper inequalities in sequence that occur for `separate_interval_set` and `split_interval_set`.

Semantics

- Concept Induction / Concept Transition
  - The semantics of itl::Maps appears to be *determined* by the *codomain type* of the map

	is model of	*if*	example
`Map<D,Monoid>`	`Monoid`		`interval_map<int,string>`
`Map<D,Set>`	`Set`	*C1*	`interval_map<int,set<int>>`
`Map<D,CommutMonoid>`	`CommutMonoid`		`interval_map<int,unsigned>`
`Map<D,AbelianGroup>`	`AbelianGroup`	*C2*	`interval_map<int,int,total>`

  - Conditions ***C1*** and ***C2*** restrict the *Concept Induction* to specific *map traits*
    - ***C1***: Value pairs that carry a *neutral element* as associated value are always deleted (Trait: ***absorbs_neutrons***).
    - ***C2***: The map *is total*: Non existing keys are implicitly mapped to *neutral elements* (Trait: ***is_total***).

Implementation

- Itl containers are implemented based on std::set and std::map
  - Basic operations like *adding* and *subtracting* intervals or interval value pairs perform with a time *complexity between** *amortized O(log n)* and *O(n)*, where *n* is the number of intervals of a container.
  - Operations like *addition* and *subtraction* of whole containers are having a worst case complexity of *O(m log(n+m))*, where *n* and *m* are the numbers of intervals of the containers to combine.

    * : Consult the library documentation for more detailed information.

Future Works

- Implementing interval_maps of sets more efficiently
- Revision of features of the extended itl (itl_plus.zip)
  - Decomposition of histories: k histories h_k with attribute types $A_1, ..., A_k$ are "*decomposed*" to a product history of tuples of attribute sets:
    $(h_1<T,A_1>,..., h<T,A_k>) \rightarrow h<T, (set<A_1>,\ldots, set<A_k>)>$
  - Cubes (generalized crosstables): Applying *aggregate on collision* to maps of tuple value pairs in order to organize hierachical data and their aggregates.

Availability

- Itl project on sourceforge (version 2.0.1)
  http://sourceforge.net/projects/itl
- Latest version on boost vault/Containers (3.1.0)
  http://www.boostpro.com/vault/ → containers
  - itl_3_1_0.zip : Core itl in preparation for boost
  - itl_plus_3_1_0.zip : Extended itl including histories, cubes and automatic validation (LaBatea).
- Online documentation at
  http://www.herold-faulhaber.de/
  - Doxygen generated docs for (version 2.0.1)
    http://www.herold-faulhaber.de/itl/
  - Latest boost style documentation (version 3.1.0)
    http://www.herold-faulhaber.de/boost_itl/doc/libs/itl/doc/html/

Availability

- Boost sandbox
  https://svn.boost.org/svn/boost/sandbox/itl/
  - Core itl: Interval containers in prepartion for boost
    https://svn.boost.org/svn/boost/sandbox/itl/boost/itl/
    https://svn.boost.org/svn/boost/sandbox/itl/libs/itl/
  - Extended itl_xt: “histories” and cubes
    https://svn.boost.org/svn/boost/sandbox/itl/boost/itl_xt/
    https://svn.boost.org/svn/boost/sandbox/itl/libs/itl_xt/
  - Validater LaBatea:
    Compiles with msvc-8.0 or newer, gcc-4.3.2 or newer
    https://svn.boost.org/svn/boost/sandbox/itl/boost/validate/
    https://svn.boost.org/svn/boost/sandbox/itl/libs/validate/